



Assessing the changes in the impacts of electricity on climate change over time and across countries: A Functional Data Analysis Approach

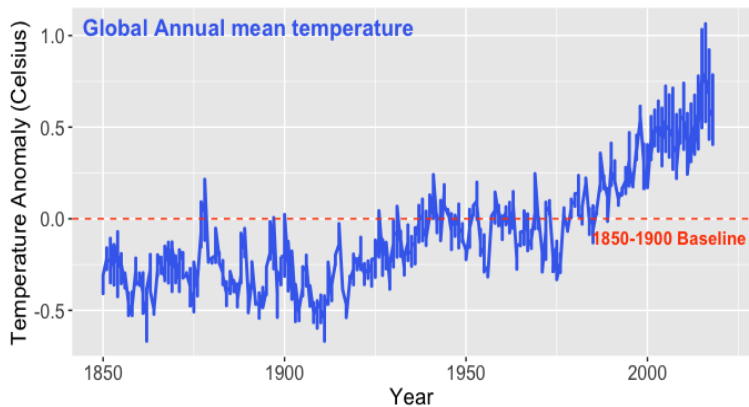
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SDG13

Taking urgent action to combat climate change and its impacts.

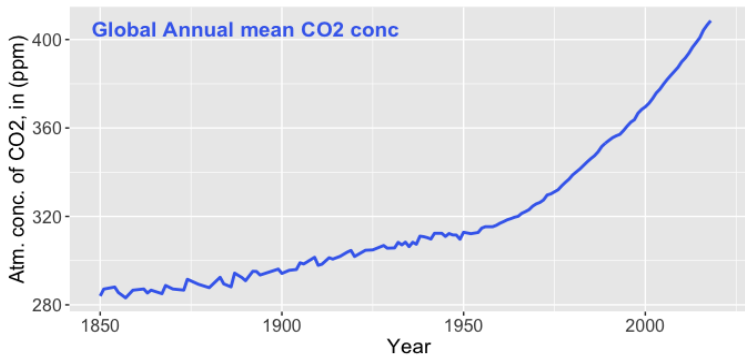


- To mitigate the impacts, we need to understand and quantify the impacts of human activities on the drivers of climate change.

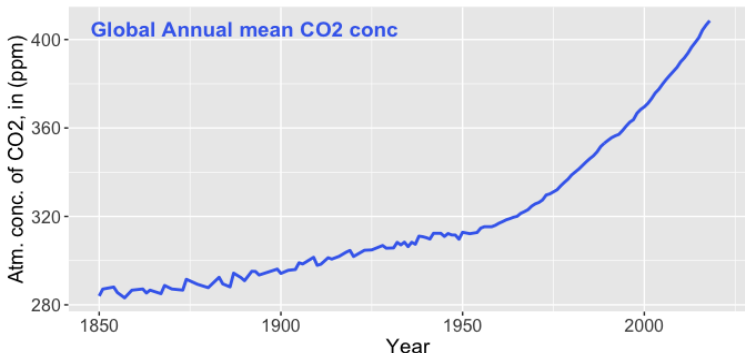


- To mitigate the impacts, we need to understand and quantify the impacts of human activities on the drivers of climate change.
- The rise in global average temperature is mainly attributed to an increase in greenhouse gas emissions, **especially CO₂**.

- Since the industrial revolution, greenhouse gas emissions have increased **exponentially and simultaneously** with energy-production.

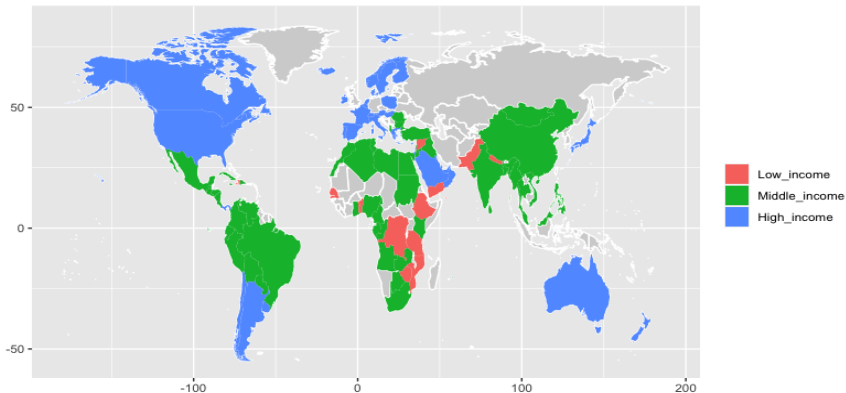


- Since the industrial revolution, greenhouse gas emissions have increased **exponentially and simultaneously** with energy-production.



- CO₂ emissions primarily stems from burning fossil fuels e.g. oil, coal and gas for energy use.
- **China** is the world's largest emitter (25%), followed by the **USA** (18%).

- **Electricity** is considered the main source of global CO₂ emissions; but this is also attributed to the methods used to produce electricity.
- Economic growth and industrial development are not the only drivers of CO₂ emissions but also **policy and technology choices**.



For 108 countries from 1975-2014:

- Annual carbon dioxide emissions (kt) per capita.
- Annual electric power consumption (kWh) per capita.

- ① Assess the discrepancies in the trends of CO₂ emissions and electricity consumption over time across countries.

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Using Functional Data Analysis

Why Functional Data Analysis?

Panel Data Analysis

- Handle data from a sample of individual units; each unit observed repeatedly over time.
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Functional Data Analysis

- Useful when dealing with highly **heterogeneous** data; allows each subject to determine its own functional structure.
- Able to handle **time-varying** relationships among variables.
- Powerful in visualizing and capturing **complex** data patterns.

In FDA, data are viewed as the realizations of a functional stochastic process $X_i(t) : i \in \mathbb{Z}, t \in \mathcal{T}$, where:

- i is a **discrete** parameter denoting **country**.
- t is a **continuous** parameter denoting **time**.
- $X_i(t)$ is obtained by **smoothing** raw data.

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Discrete data

country ₁	$x_{1,1}$	$x_{1,2}$...	$x_{1,m}$
country ₂	$x_{2,1}$	$x_{2,2}$...	$x_{2,m}$
⋮	⋮	⋮	⋮	⋮
⋮	⋮	⋮	⋮	⋮
country _{n}	$x_{n,1}$	$x_{n,2}$...	$x_{n,m}$

set of points in \mathbb{R}^p

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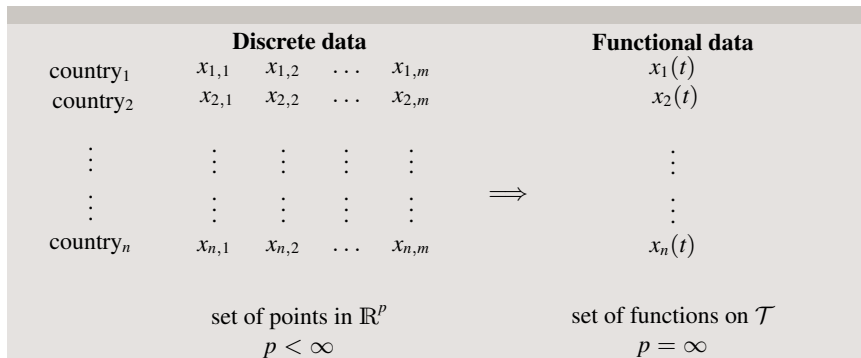
⇒

set of points in \mathbb{R}^p
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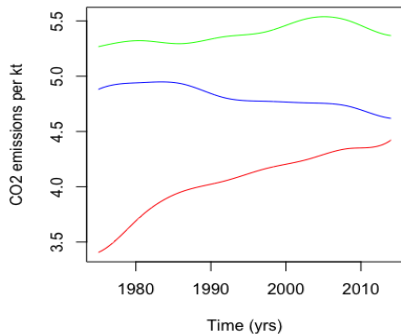
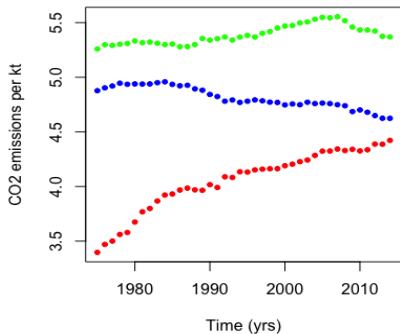
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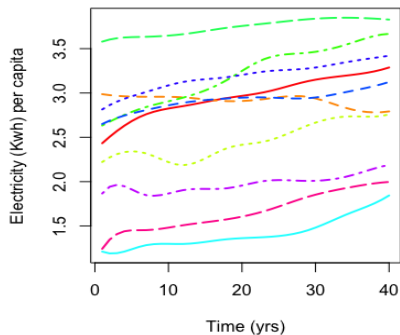
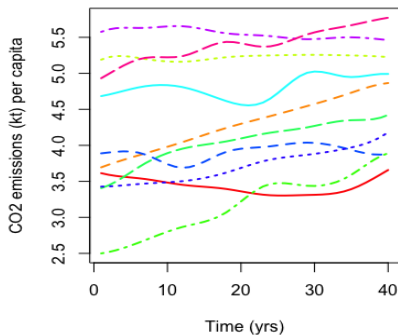
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- **Functional Principal Component Analysis**

- Identify the primary sources of variations in a set of curves.

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- Identify the primary sources of variations in a set of curves.
⇒ What are the sources of differences between countries' trends?

- **Functional Regression**

- Explain how relationships between (functional) response and explanatory vars varied over the functional domain (time).
⇒ How the relationship between electricity consumption and CO₂ emissions evolved over time?

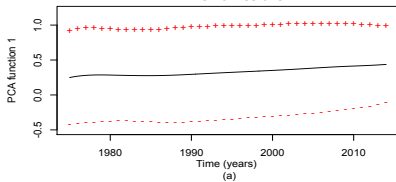
FPCs are obtained via the eigen-decomposition of the covariance

$$\int v(s, t)\xi(t)dt = \lambda\xi(s),$$

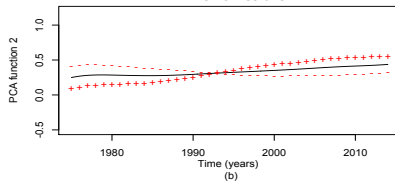
where

- $v(s, t)$ is the **covariance function** across curves between time points s and t .
- λ and $\xi(\cdot)$ are the eigenvalues and **eigenfunctions** obtained such that λ_j (non-decreasing) > 0 ; $\int_{\mathcal{T}} \xi_j^2(t)dt = 1$; $\int_{\mathcal{T}} \xi_j(t)\xi_{j'}(t)dt = 0$

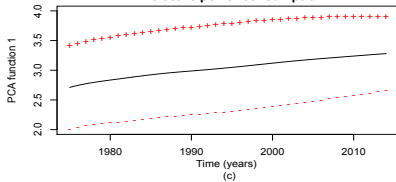
**% of variability explained 97.4
in CO2 emissions**



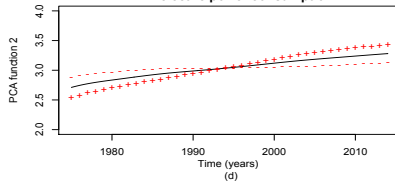
**% of variability explained 1.9
in CO2 emissions**

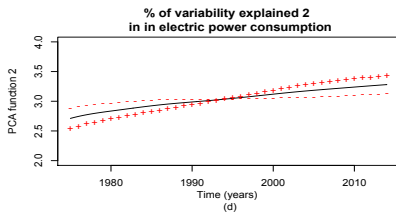
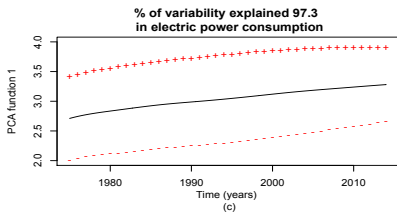
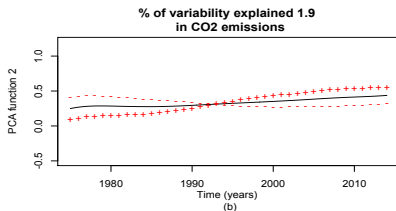
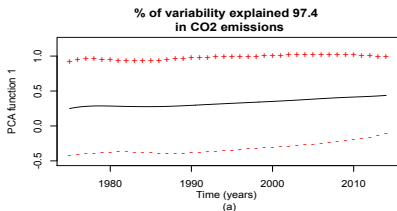


**% of variability explained 97.3
in electric power consumption**



**% of variability explained 2
in electric power consumption**

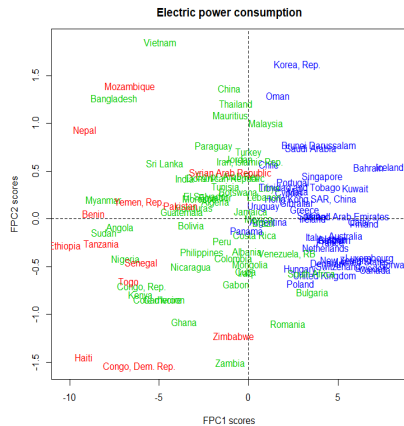
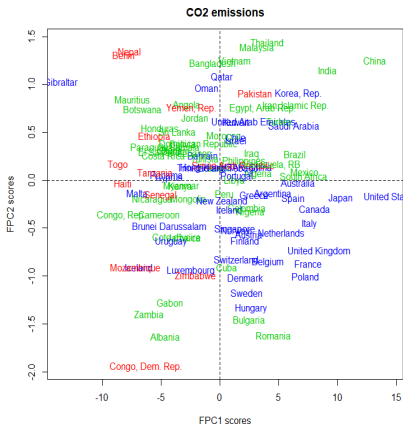


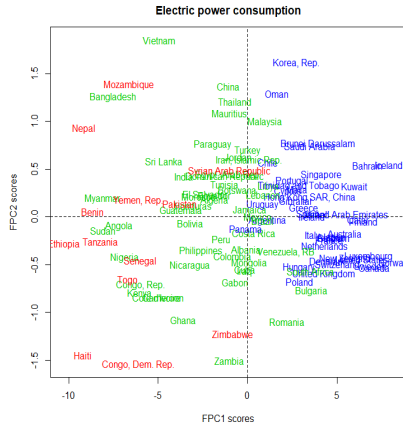
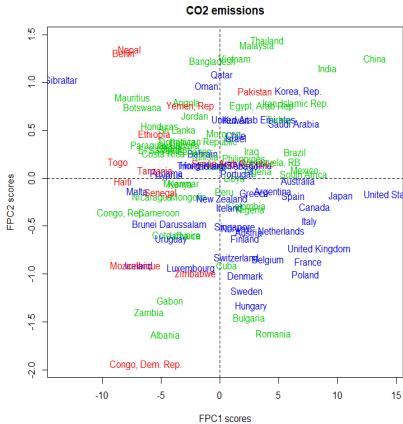


Discrepancies between countries' trends are attributed to:

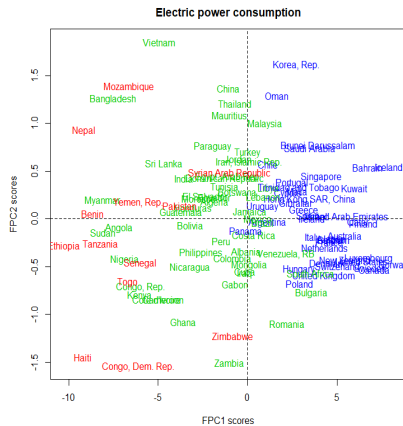
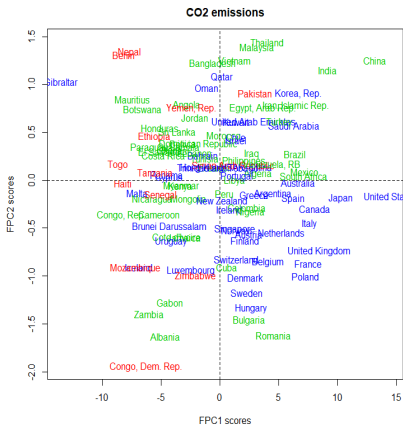
- the deviations from the mean level; and
- the contrast between the period 1975 - 1990 and post 1990.

FPCA (Results)

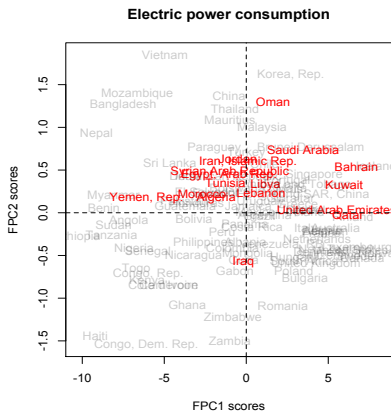
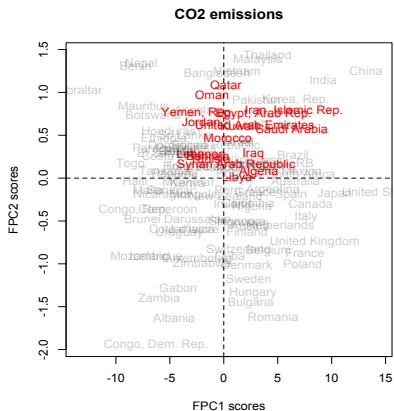




- Despite increasing electric consumption, high-income European countries managed to reduce their CO₂ emissions over time (esp. after 1990).



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- **China, India and Gulf countries** continue to emit high CO₂ emissions.



- **All MENA countries** continually emit increasing CO₂ emissions regardless of income group; highlighting consequences of development.

The model of interest here is:

$$\text{CO2}_i(t) = \beta_0(t) + \beta_1(t)\text{Electric Consumption}_i(t) + \beta_2(t)\text{GDP}_i(t) + \epsilon_i(t),$$

where $\beta_0(t)$, $\beta_1(t)$, $\beta_2(t)$ are the regression coefficients **functions**.

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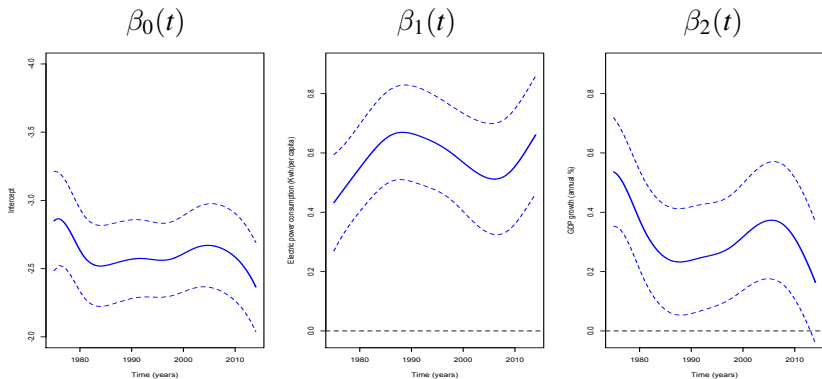
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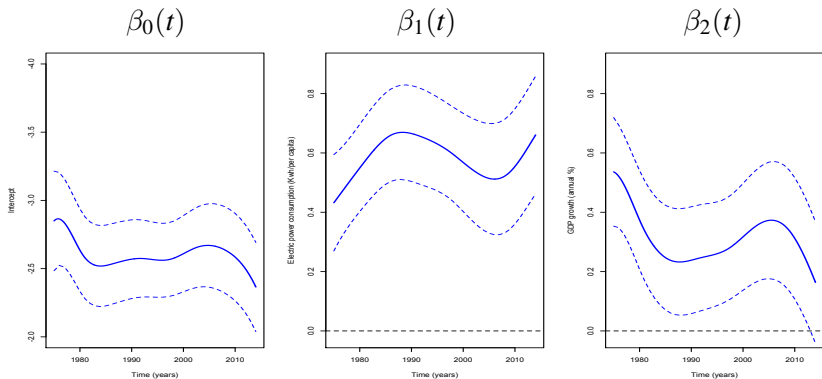
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- It has both the response and the covariates as **functions of time**.
- It relates the response function **at a specific point** to the covariate value **at the same point**.

Functional Regression (Results)

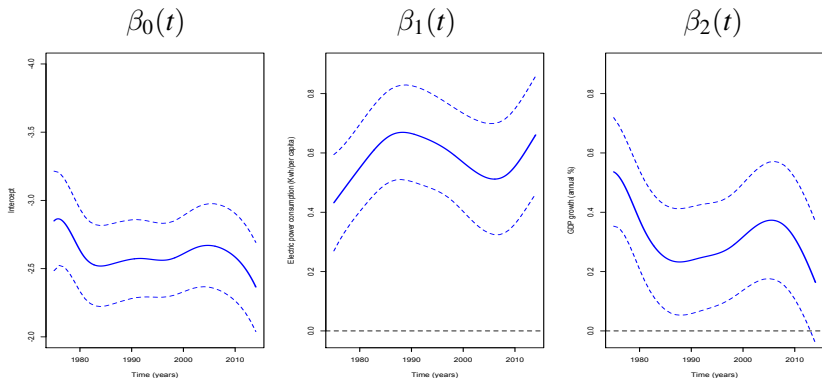


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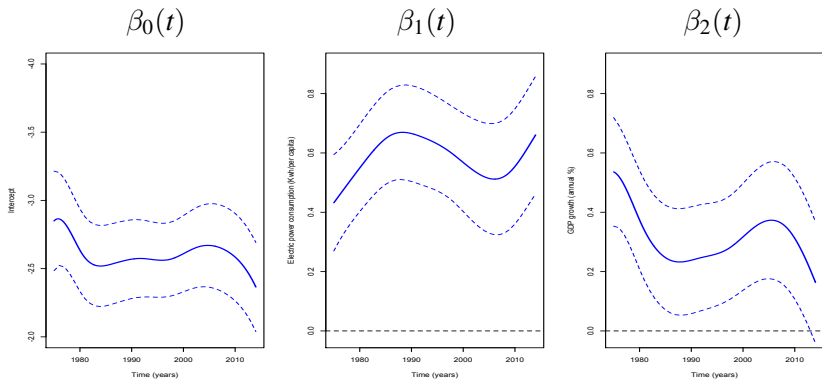
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- The influence of electricity **dropped between 1990 and 2006** and increased slightly afterwards.

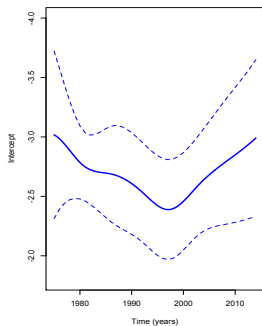
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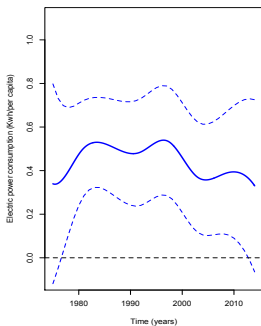
- The influence of electric consumption and GDP on CO₂ emissions **vary over time**.
- The influence of electricity **dropped between 1990 and 2006** and increased slightly afterwards.
- The influence of GDP **increased between 1990 and 2006** then started to drop afterwards.

Functional Regression - MENA region (Results)

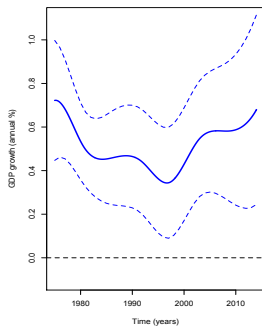
$\beta_0(t)$



$\beta_1(t)$

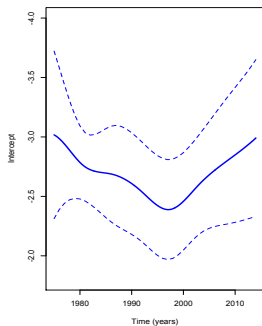


$\beta_2(t)$

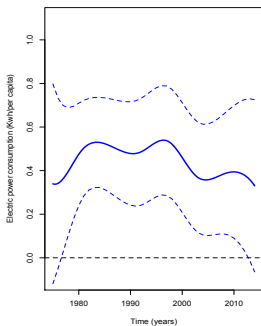


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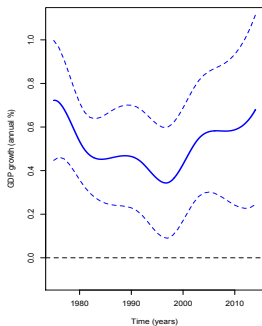
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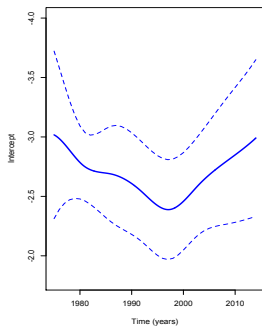
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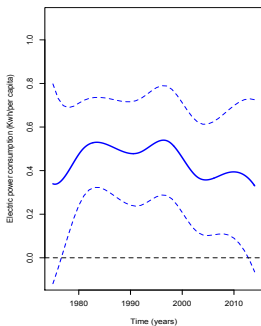
- Average CO₂ increases since 2000 simultaneously with an increase in the influence of GDP. **(Reforms + Early stage of EKC)**

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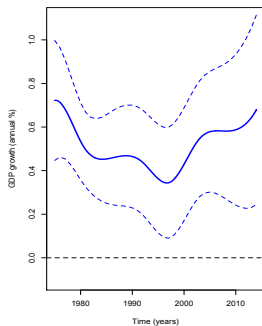
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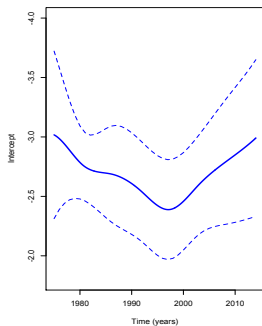
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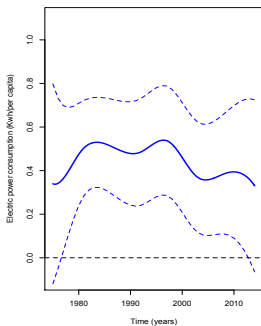
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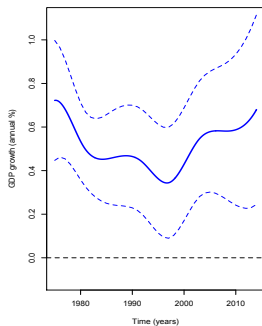
$\beta_0(t)$



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- Average CO₂ increases since 2000 simultaneously with an increase in the influence of GDP. **(Reforms + Early stage of EKC)**
- The influence of electric consumption remains almost the same over the study period.
- More variability between MENA region countries in the recent years.

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Policy implications

- Incentivise industries to adopt more energy efficient technologies.
- Increase the capacity of renewables (Windfarms and Solar electricity). Expensive!
- Targeted investment in innovation - opportunities for new business, exports, jobs and a cleaner environment.